

NumberWonders Fibonacci and Pattern Puzzle Pack v1

Pilot release - direct download edition

This pack helps grades 4-8 learners build sequence fluency, pattern reasoning, and rule-explanation skills through Fibonacci-focused puzzles and visual tasks.

Estimated Time: 10 sessions x 30-45 min

Format: Printable worksheet + puzzle board pack

Audience: Classrooms, clubs, homeschool enrichment

License: One classroom or one household

Fibonacci

Sequences

Visual patterns

Reasoning

Answer key included

Teacher Quick Start

- 1. Use one worksheet as warmup and one as challenge each session.
- 2. Ask students to state the pattern rule in words before calculating.
- 3. Compare two different valid methods after each puzzle.
- 4. Use the challenge board tasks for stations or homework.

Facilitation tip: Require one sentence of justification for every sequence answer. This boosts transfer and confidence.

Worksheet Index

| # | Topic | Target Skill |
|----|------------------------------|--------------------------|
| 1 | Fibonacci Basics | Generate terms from rule |
| 2 | Is It Fibonacci? | Membership checks |
| 3 | Recursive and Explicit Clues | Rule interpretation |
| 4 | Pattern Machines | Input/output reasoning |
| 5 | Visual Dot Patterns | Figure growth analysis |
| 6 | Golden Ratio Approximations | Ratio behavior |
| 7 | Number Pattern Puzzles | Mixed sequence logic |
| 8 | Word Problems with Sequences | Modeling contexts |
| 9 | Pattern Proof Starters | Explain and justify |
| 10 | Fibonacci Challenge Board | Extended puzzles |

Worksheet 1: Fibonacci Basics

Complete each sequence using $F(n)=F(n-1)+F(n-2)$.

- 1) 0, 1, 1, 2, 3, __, __, __
- 2) 1, 1, 2, 3, 5, __, __
- 3) 2, 3, 5, 8, 13, __, __
- 4) 5, 8, 13, 21, __, __
- 5) 13, 21, 34, __, __, __
- 6) 34, 55, 89, __, __
- 7) 3, 5, 8, 13, __, __
- 8) 8, 13, 21, 34, __, __

Worksheet 2: Is It Fibonacci?

Mark Yes/No and justify your answer for four numbers.

- 1) 21: Yes / No
- 2) 22: Yes / No
- 3) 34: Yes / No
- 4) 35: Yes / No
- 5) 55: Yes / No
- 6) 56: Yes / No
- 7) 89: Yes / No
- 8) 90: Yes / No

Worksheet 3: Recursive and Explicit Clues

Find the next terms and identify the rule style.

- 1) 4, 7, 11, 18, 29, __, __
- 2) 2, 6, 12, 20, 30, __, __
- 3) 1, 4, 9, 16, 25, __, __
- 4) 3, 6, 12, 24, 48, __, __
- 5) 5, 9, 14, 23, 37, __, __
- 6) 10, 7, 11, 8, 12, 9, __, __

Worksheet 4: Pattern Machines

Use each rule machine to fill outputs.

| Input n | Rule | Output |
|---------|-------------------|--------|
| 1 | $2n + 1$ | __ |
| 2 | $2n + 1$ | __ |
| 3 | $2n + 1$ | __ |
| 4 | $n^2 + 1$ | __ |
| 5 | $n^2 + 1$ | __ |
| 6 | $n^2 + 1$ | __ |
| 7 | Fibonacci index n | __ |
| 8 | Fibonacci index n | __ |

Worksheet 5: Visual Dot Patterns

Count dots by pattern, then predict figure 6.

Pattern A counts by +3 each step starting at 2: figure 1..5 = _____

Pattern B is square numbers: figure 1..5 = _____

Pattern C follows Fibonacci: figure 1..7 = _____

For Pattern A, figure 6 = ____ ; Pattern B figure 6 = ____ ; Pattern C figure 8 = ____

Extension: Draw a dot sketch for one of the sequences and explain the growth.

Worksheet 6: Golden Ratio Approximations

Compute each ratio $F(n+1)/F(n)$ and observe the trend.

1) $2/1 =$ _____

2) $3/2 =$ _____

3) $5/3 =$ _____

4) $8/5 =$ _____

5) $13/8 =$ _____

6) $21/13 =$ _____

7) $34/21 =$ _____

8) $55/34 =$ _____

What value do these seem to approach? _____

Worksheet 7: Number Pattern Puzzles

Find the missing number or expression.

1) 7, 10, 13, 16, ____

2) 3, 6, 12, 24, ____

3) 1, 1, 2, 3, 5, 8, ____

4) 2, 5, 10, 17, 26, ____

5) 81, 27, 9, 3, ____

6) 4, 9, 16, 25, 36, ____

7) 2, 4, 7, 11, 16, ____

8) 5, 9, 14, 20, 27, ____

Worksheet 8: Word Problems with Sequences

Build an equation and solve.

1. A rabbit model follows Fibonacci births: 1,1,2,3,5,... How many in month 8?
2. A staircase pattern adds 2 tiles each step starting with 3. How many at step 12?
3. A club doubles members every week starting at 4. How many after 6 weeks?
4. A square garden grows by one ring each season. If side lengths are 1,3,5,7,... what is side at season 10?

Worksheet 9: Pattern Proof Starters

Complete each explanation sentence.

1) This sequence is arithmetic because _____

2) This sequence is geometric because _____

3) Fibonacci differs from arithmetic because _____

4) To verify a term belongs to a sequence, I should _____

5) A visual model helps because _____

6) If two rules fit early terms, we can decide by _____

Worksheet 10: Fibonacci Challenge Board

Solve any 8 tasks.

- 1) Write Fibonacci terms from F1 to F12.
- 2) Find two consecutive Fibonacci numbers whose ratio is closest to 1.62.
- 3) Build a sequence with rule $a(n)=a(n-1)+3$ starting from 2.
- 4) Build a sequence with rule $a(n)=2a(n-1)$ starting from 3.
- 5) Which grows faster after 10 terms: Fibonacci or powers of 2?
- 6) Write an explicit formula for sequence 5,9,13,17,...
- 7) Give one real-world pattern that is approximately Fibonacci-like.
- 8) Create a 6-term puzzle sequence for a partner to solve.
- 9) Decide whether 144 is Fibonacci and justify.
- 10) Explain one common mistake when extending sequences.

Answer Key

Worksheet 1

1) 5,8,13 2) 8,13 3) 21,34 4) 34,55 5) 55,89,144 6) 144,233 7) 21,34 8) 55,89

Worksheet 2

1 Yes 2 No 3 Yes 4 No 5 Yes 6 No 7 Yes 8 No

Worksheet 3

1) 47,76 2) 42,56 3) 36,49 4) 96,192 5) 60,97 6) 13,10

Worksheet 4

$2n+1$ outputs: 3,5,7 ; n^2+1 outputs for 4,5,6: 17,26,37 ; Fibonacci index 7 and 8: 13,21

Worksheet 5

Pattern A: 2,5,8,11,14 ; Pattern B: 1,4,9,16,25 ; Pattern C: 1,1,2,3,5,8,13 ; next values A6=17, B6=36, C8=21

Worksheet 6

1) 2.00 2) 1.50 3) 1.67 4) 1.60 5) 1.625 6) 1.615 7) 1.619 8) 1.618 ; approaches about 1.618

Worksheet 7

1) 19 2) 48 3) 13 4) 37 5) 1 6) 49 7) 22 8) 35

Worksheet 8

1) 21 2) 25 3) 256 4) 19

Worksheet 9

Open responses. Key points: arithmetic has constant difference, geometric has constant ratio, Fibonacci uses two previous terms.

Worksheet 10

Sample outcomes: F1..F12 = 1,1,2,3,5,8,13,21,34,55,89,144 ; ratio close to 1.62 from 55/34, 89/55, etc.; 144 is Fibonacci (F12).

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